



Modeling of Scope Performance in Turbulence



Turbulence

Notes on this briefing



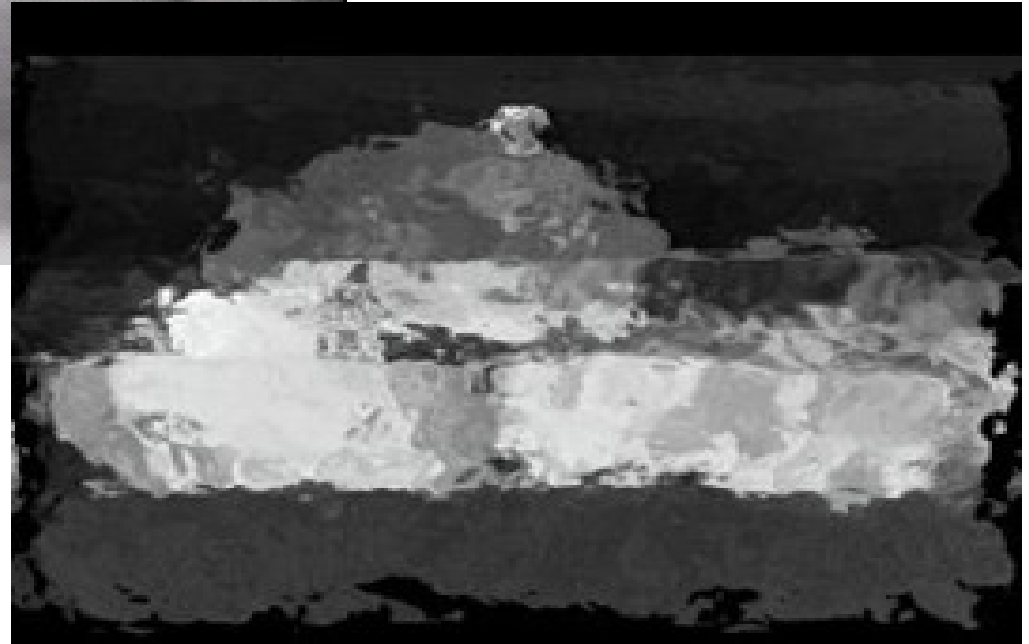
- **The NVTherm model has NOT been developed to address the ansioplanatism. There are no fielded tactical systems with turbulence mitigation exploiting this aspect.**

- **NVThermIP has limited application to SRVS BAA to:**

- Demonstrate current day optic technology will support facial ID, BUT NOT in turbulence.
- Estimate resolution required to perform basic facial ID test (BAA Preps).
- Use in designing parts of the scope itself, not the processing.
- NVThermIP will NOT be applied to evaluate the image processing aspect of the SRVS systems or proposed processing concepts.



Turbulence Impacts





Turbulence



Ultra-narrow field-of-view (UNFOV)
camera's resolution performance can be
limited by atmospheric turbulence blur
Observer Target Acquisition performance
is degraded by turbulence blur/distortion
Short Integration Time blur is
instantaneous
Long Integration Time blur is spot
"wandering"



Turbulence

MTF_{turb} model



$$\text{MTF}_{\text{short}} = \exp \{ 57.4 a \xi^{5/3} C_n^2 \lambda^{-1/3} R [1 - \mu (\xi \lambda / D)^{1/3}] \}$$

Where:

a is a wave shape constant (unity for plane wave and 3/8 for spherical)

ξ is the spatial frequency in cycles per milliradian

C_n^2 is index of refraction structure parameter

λ is the wavelength

R is the path length

D is the imaging sensor aperture diameter

μ is 0.5 in the far field and 1 in the near field.



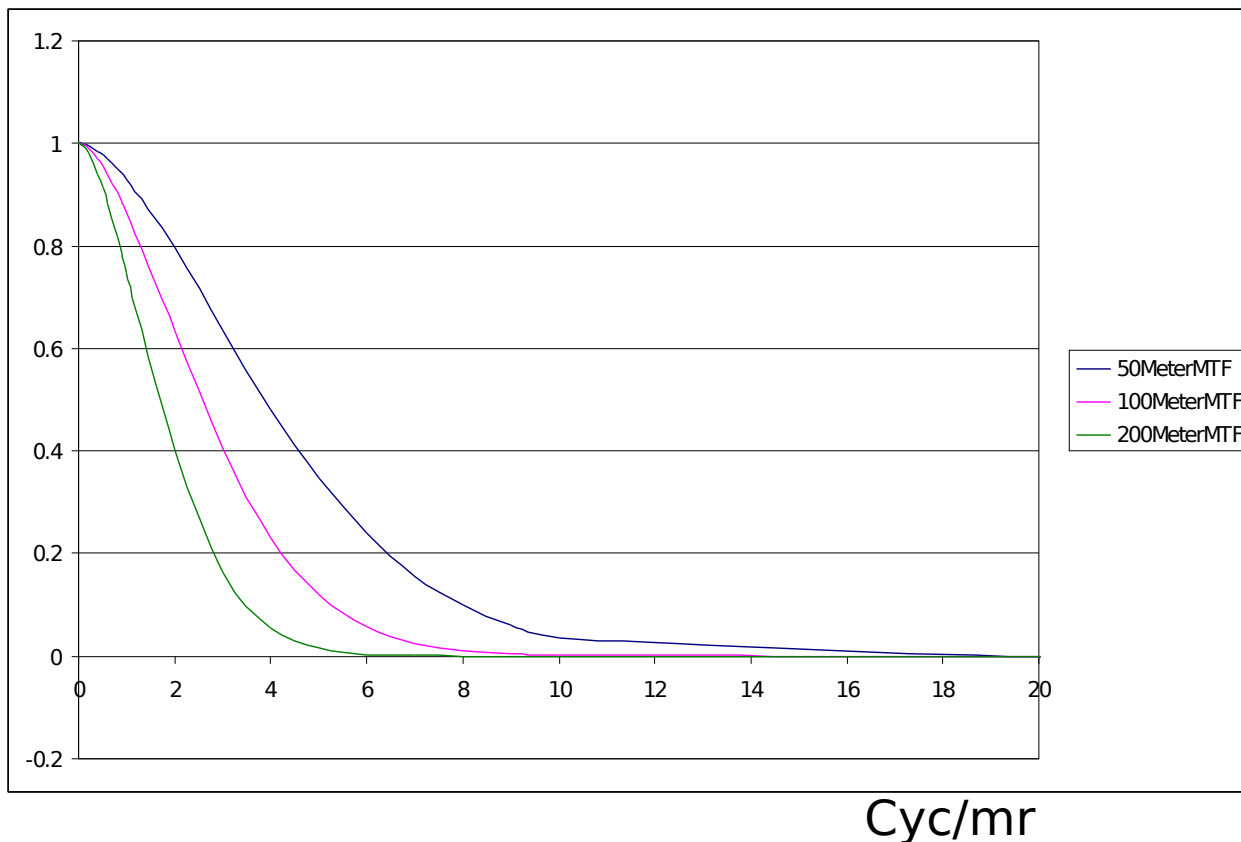
Turbulence MTF



Blur is “range dependent”

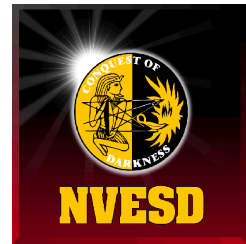
$$C_n^2 = 5 \times 10^{-13} \text{m}^{(2/3)}, D = 60 \text{mm}$$

MTF

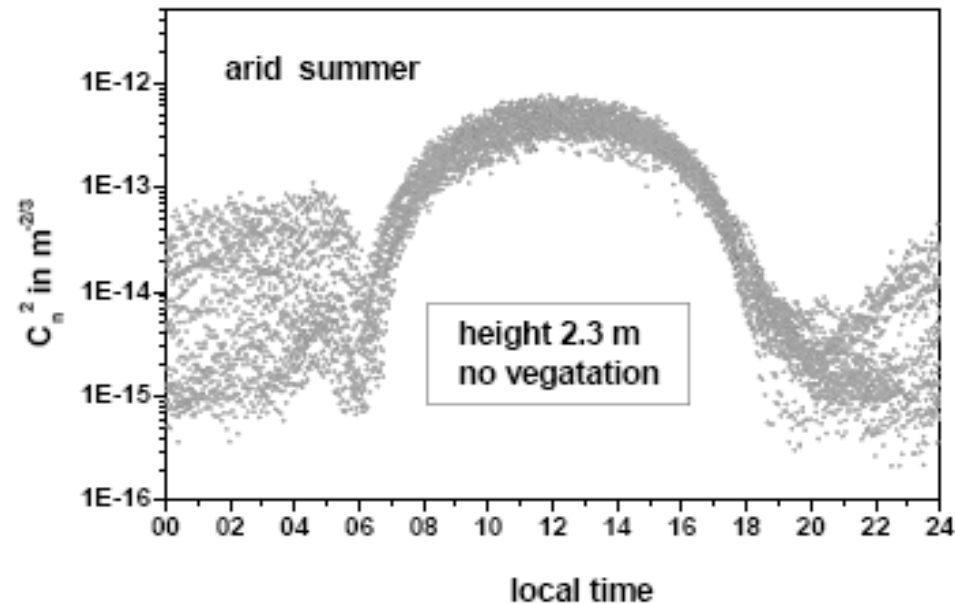
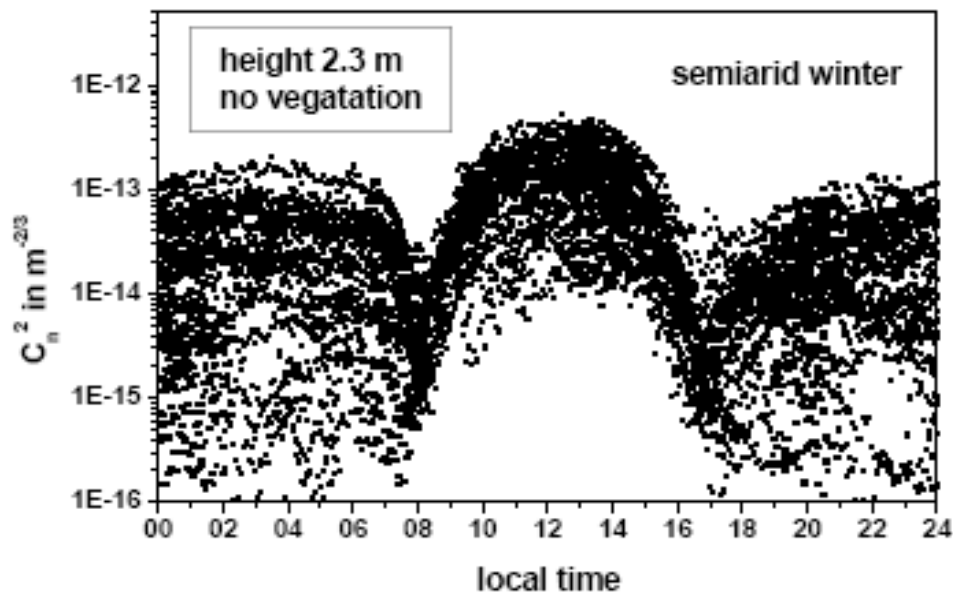




Turbulence

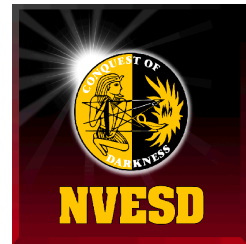


Weiss-Wrana's data showed a characteristic day/night variation when temperatures were moderate:

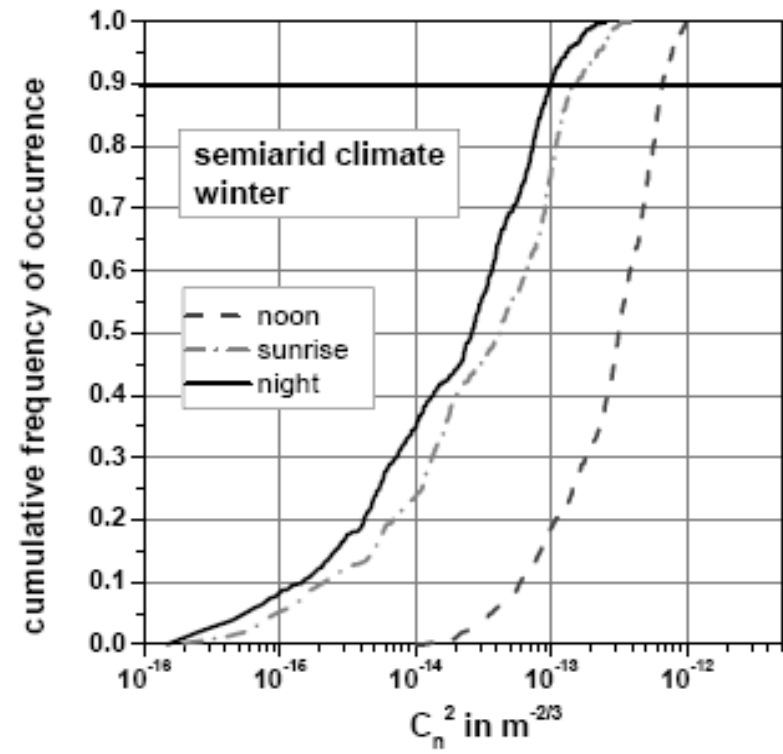
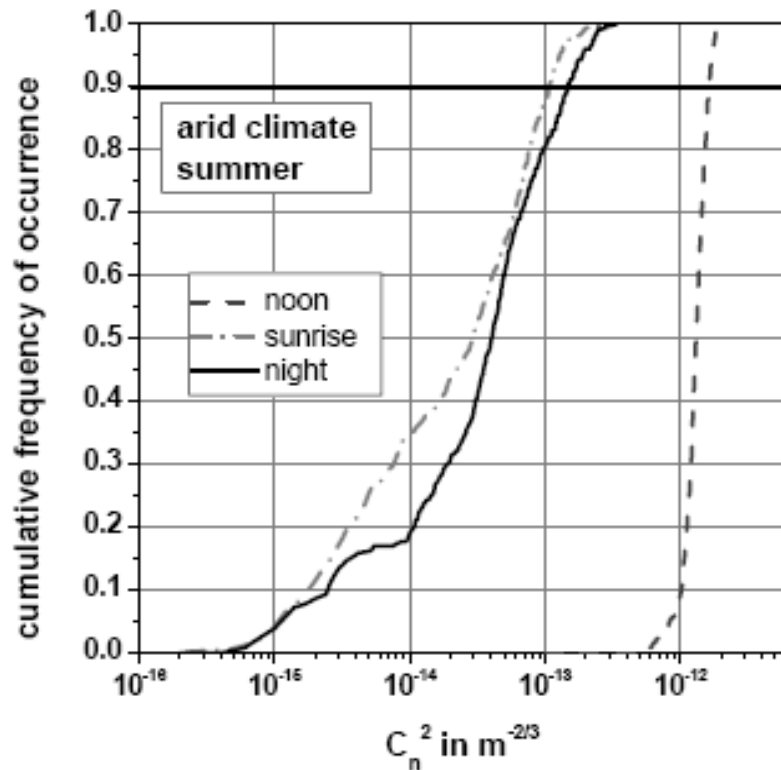




Turbulence



Sample frequency of occurrence plots derived from the raw C_n^2 data:

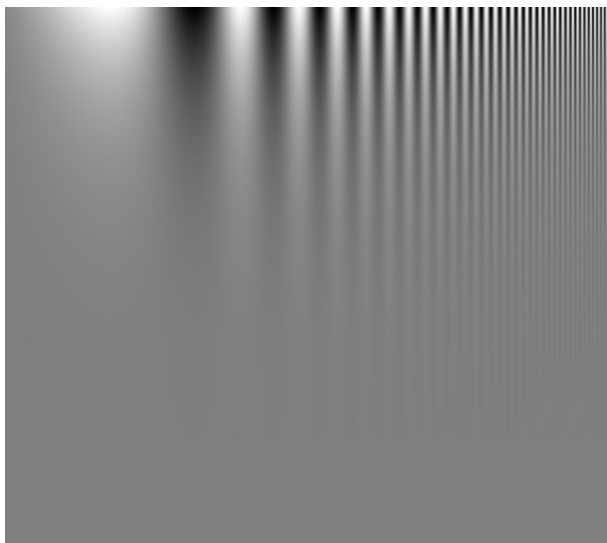




Contrast Threshold Function



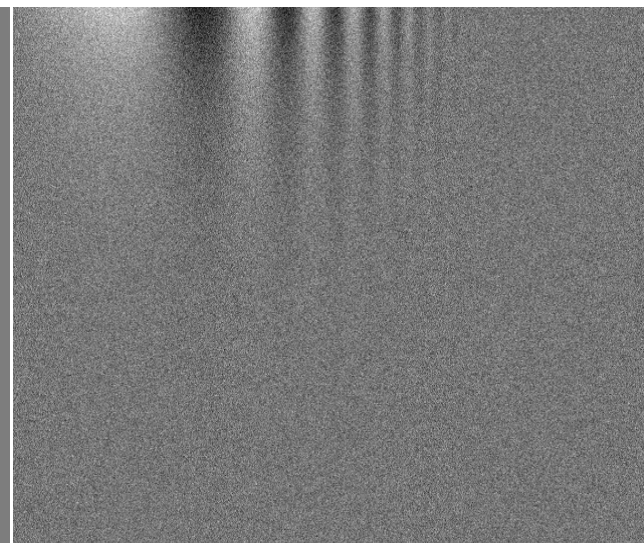
Eye

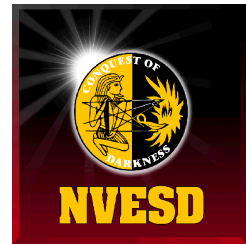


Eye + Blur



Eye + Blur + Noise





System CTF

Measured
threshold of naked
eye

Noise on display
filtered by eye

$$CTF_{sys}(\xi) = \frac{CTF(\xi)}{MTF(\xi)} \left[1 + \frac{\alpha^2 \sigma^2(\xi)}{S_{tmp}^2} \right]^{1/2}$$

Blur caused by
system

Temp that generates average
display brightness

ξ = spatial frequency in (milliradian)⁻¹

$MTF(\xi)$ is system modulation transfer function

$\sigma(\xi)$ = noise filtered by display & visual system in units of Kelvin

α is a calibration constant with **units root-Hertz**

S_{tmp} units Kelvin (scene temperature that results in average display luminance)



Target Acquisition



Source Contrast:

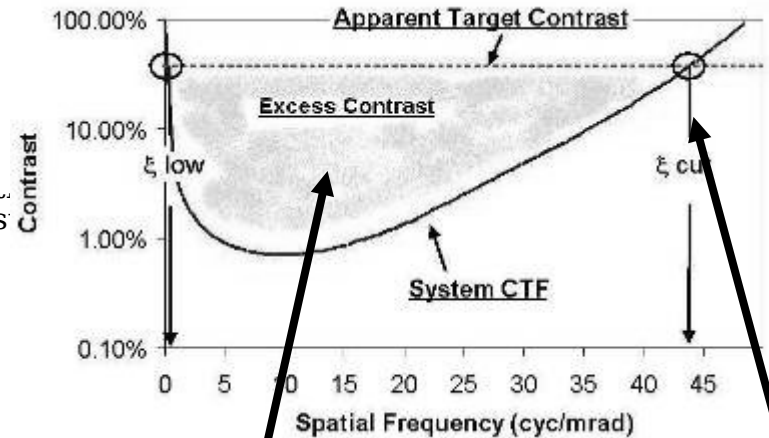
$$C_{\text{char. Dim.}} = \sqrt{\text{Area}_{\text{tgt}}}$$



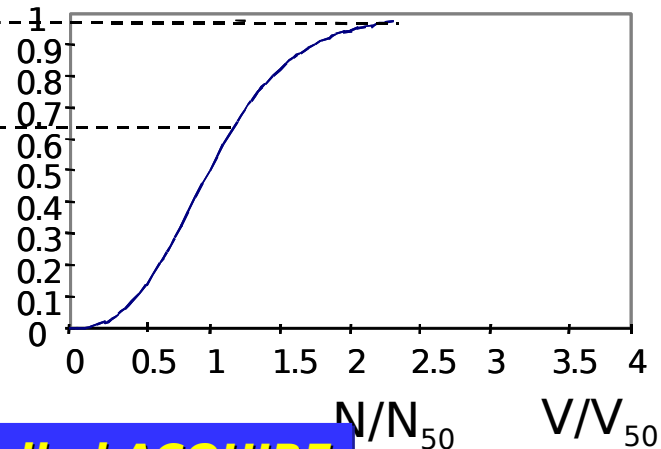
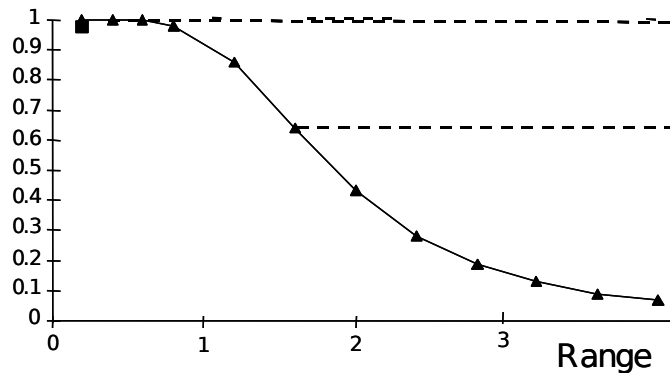
Atmospheric
Transmission



Range to Sensor (R)



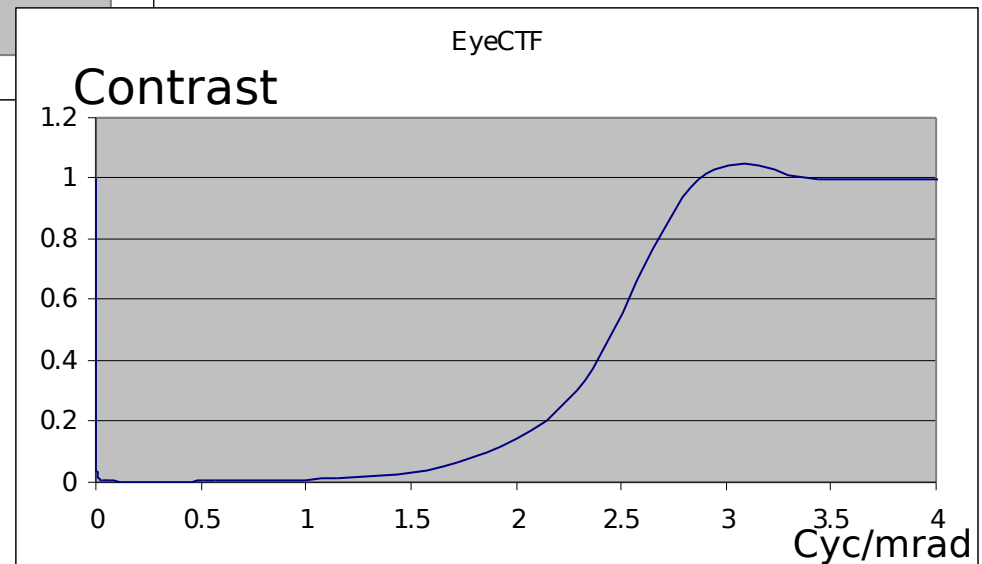
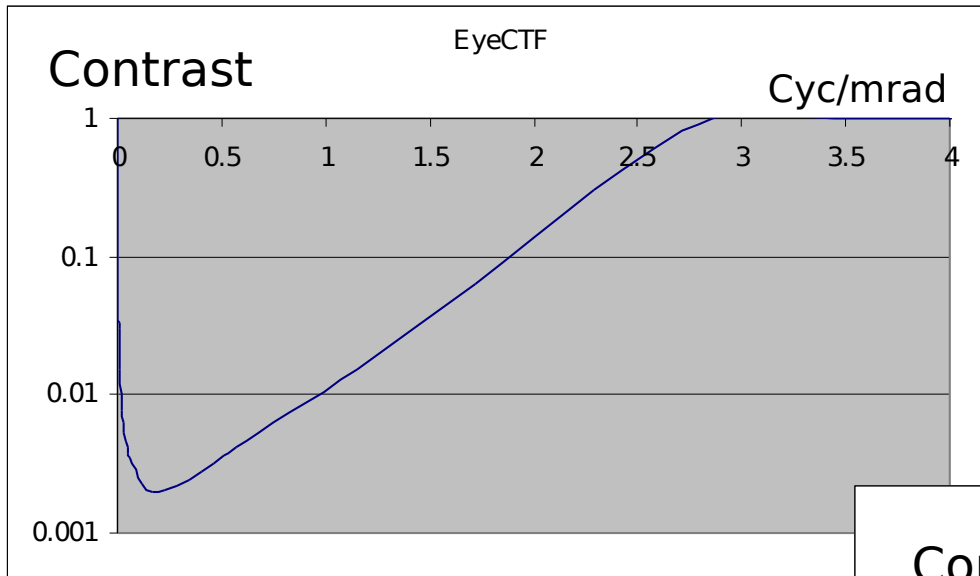
$$V = \int_{\xi_{\text{low}}}^{\xi_{\text{cut}}} \sqrt{\frac{C(\xi)}{CTF(\xi)}} d\xi \left[\frac{s}{R} \right] \quad \text{or} \quad N = \xi_{\text{cut}} \left[\frac{s}{R} \right]$$



N50, and Limiting Frequency Version is Called ACQUIRE

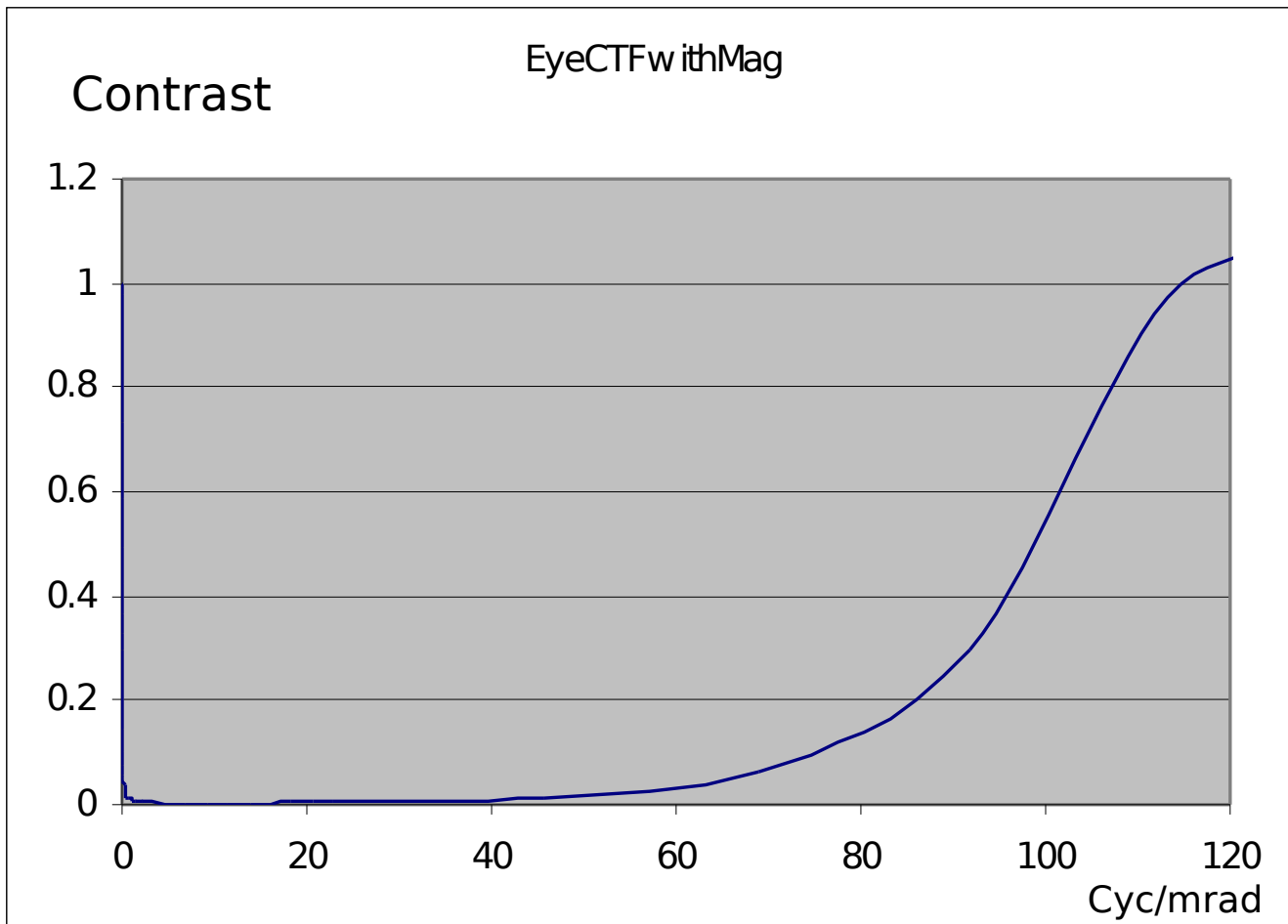


Eye CTF





Eye CTF With 40X Mag





Cycles on Face for 90% Prob ID



It has been roughly determined that a 40X, 60mm spotter scope
can ID a human face at 1000m

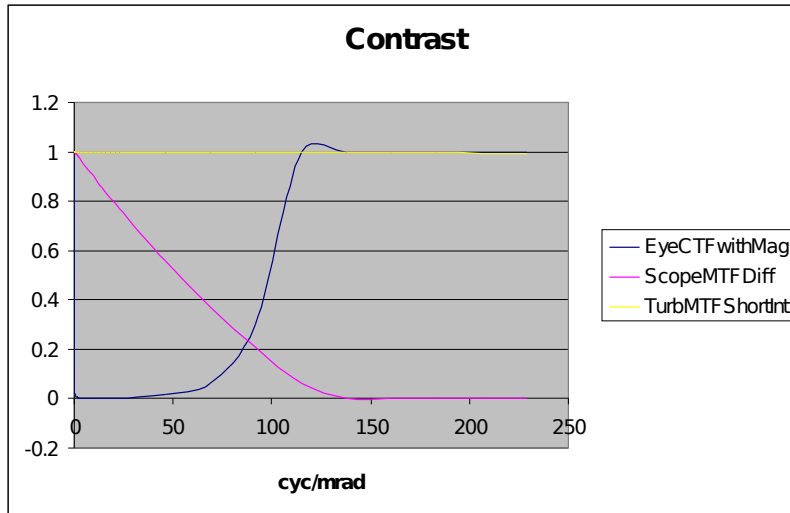
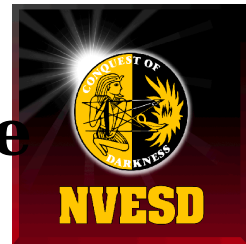
Facial Dimension is estimated at 7 inches by 9 inches
Equal to 406cm^2
Characteristic Dimension is 20cm

We will do this in terms of N50 and V50

This estimate was related to extremely low turbulence



90% Facial ID W/No Turbulence



60mm Aperture

40X Mag

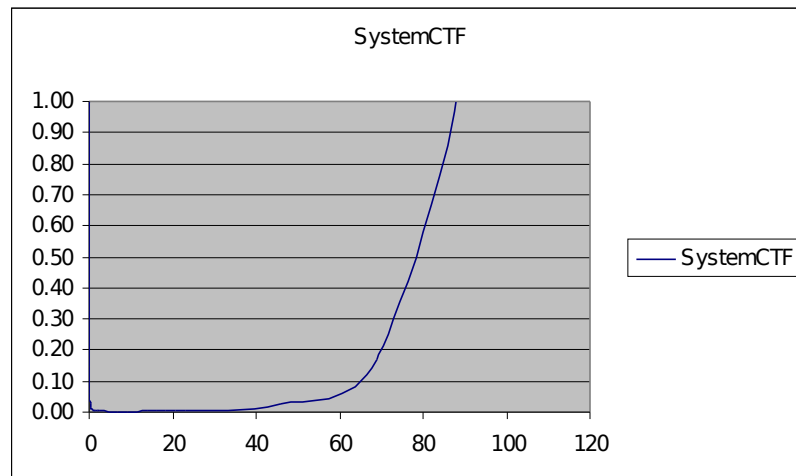
Lim Freq at 0.2 Contrast = 70 cyc/mrad

N90

Frequency is $70 \text{ cyc/mrad} \times 0.2 \text{ mrad}$
= 14 cycles on target

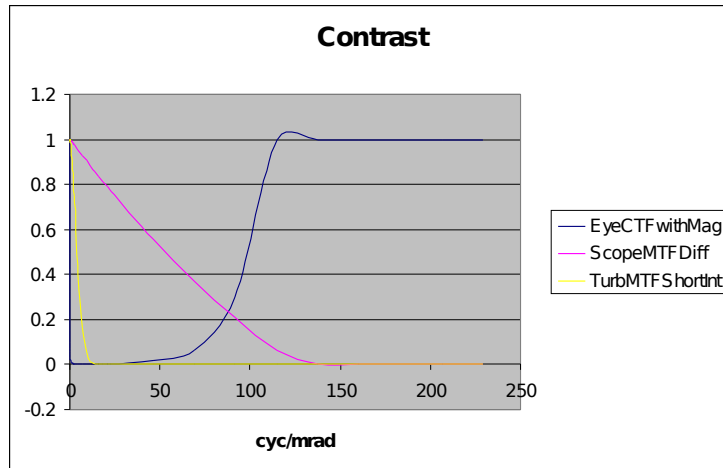
V90

Frequency is $280 \text{ cyc/mrad} \times 0.2 \text{ mrad}$
= 55 cycles on target

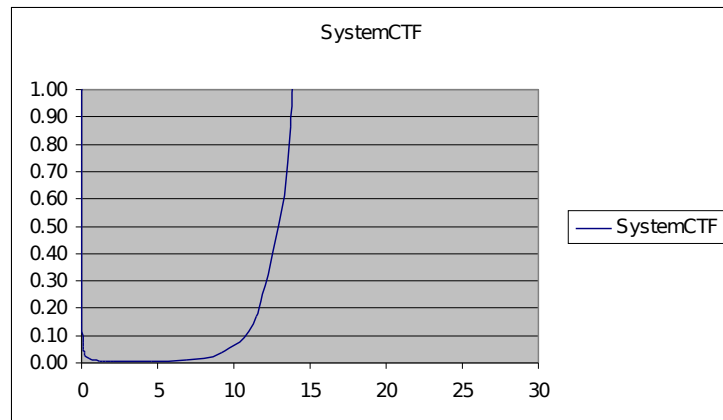




Range Prediction for 90% Facial ID W/5E-13 m(-2/3) CN2

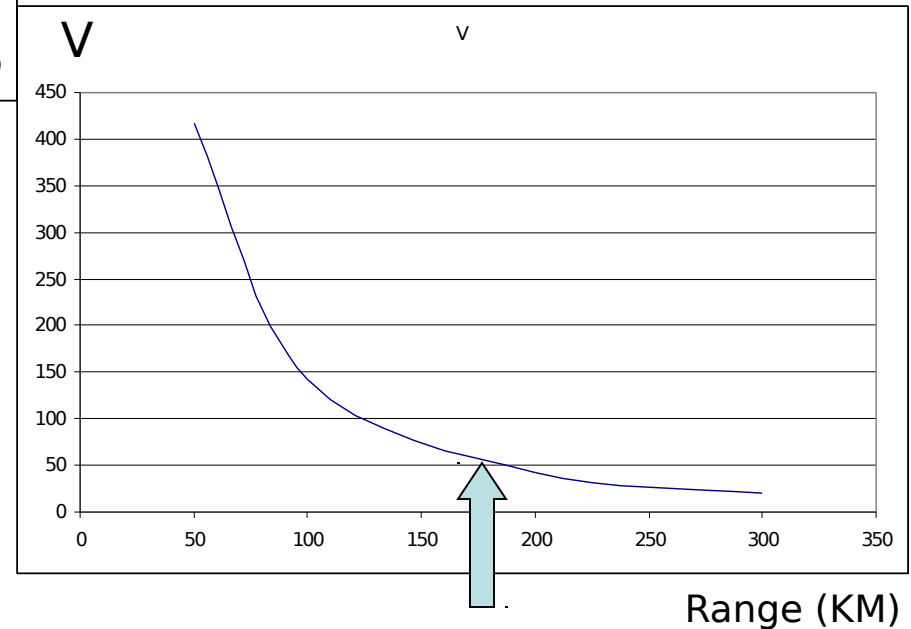
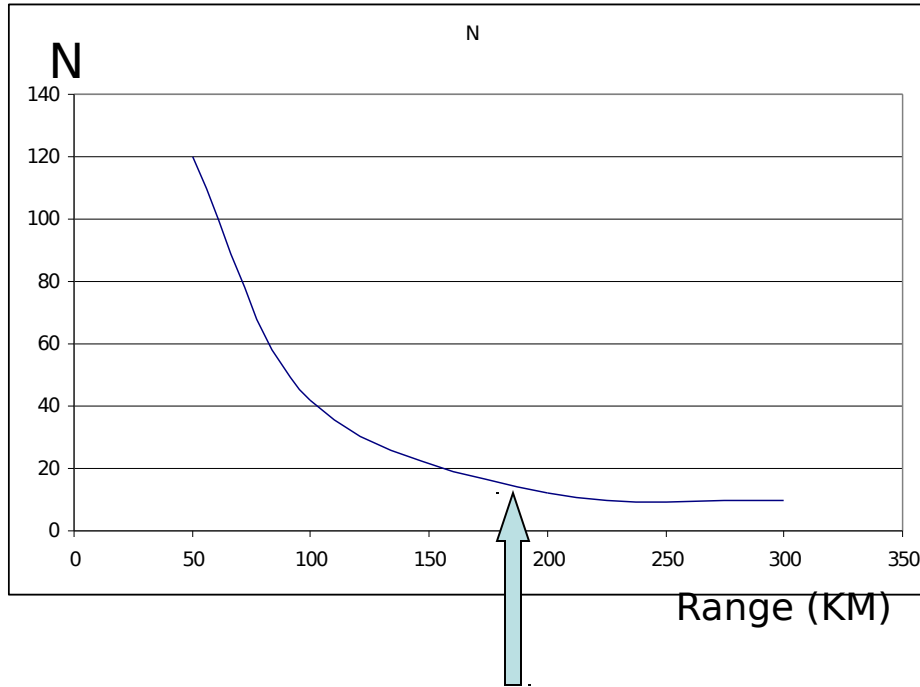


Note the Significant Reduction in the CTF of the System Due to the Turbulence MTF (200 meters shown)





Range Prediction for 90% Facial ID W/5E-13 m(-2/3) CN2





Conclusion



- Demonstrates current day optic technology will support facial ID, BUT NOT in turbulence.
- Estimates resolution required to perform basic facial ID test (for BAA Preps).
- Possibly useful model in designing elements of the scope itself